

Další seminář z algebry se koná 26.11.2020 od 13.00 online na platformě [ZOOM](#). Informace pro připojení a další program semináře je [zde](#).

**Martin Bidlingmaier** (Aarhus University)

Model categories of lcc categories and the gros model of dependent type theory

Abstrakt:

In this talk we discuss various model categories of locally cartesian closed (lcc) categories and their relevance to coherence problems, in particular the coherence problem of categorical semantics of dependent type theory. We begin with  $Lcc$ , the model category of locally cartesian closed (lcc) sketches. Its fibrant objects are precisely the lcc categories, though without assigned choices of universal objects. We then obtain a Quillen equivalent model category  $sLcc$  of strict lcc categories as the category of algebraically fibrant objects of  $Lcc$ . Strict lcc categories are categories with assigned choice of lcc structure, and their morphisms preserve these choices on the nose. Conjecturally,  $sLcc$  is precisely Lack's model category of algebras for a 2-monad  $T$ , where  $T$  is instantiated with the free lcc category functor on  $Cat$ . We then discuss the category of algebraically cofibrant objects of  $sLcc$  and show how it can serve as a "gros" model of dependent type theory.